# Three New Probabilistic Models for Dependency Parsing: An Exploration* 

Jason M. Eisner<br>CIS Department, University of Pennsylvania<br>200 S. 33rd St., Philadelphia, PA 19104-6389, USA<br>jeisner@linc.cis.upenn.edu


#### Abstract

After presenting a novel $O\left(n^{3}\right)$ parsing algorithm for dependency grammar, we develop three contrasting ways to stochasticize it. We propose (a) a lexical affinity model where words struggle to modify each other, (b) a sense tagging model where words fluctuate randomly in their selectional preferences, and (c) a generative model where the speaker fleshes out each word's syntactic and conceptual structure withont regard to the implications for the hearer. We also give preliminary empirical results from evaluating the three models' parsing performance on annotated Wall Street Journal training text (derived from the lenn Treebank). In these results, the generative model performs significantly better than the others, and does about equally well at assigning part-of-speech tags.


## 1 Introduction

In recent years, the statistical parsing community has begun to reach out for syntactic formalisms that recognize the individuality of words. Link grammars (Sleator and Temperley, 1991) and lexicalized tree-adjoining grammars (Schabes, 1992) have now received stochastic treatments. Other researchers, not wishing to abandon context-freo grammar (ClG) but disillusioned with its lexical blind spot, have tried to re-parameterize stochastic CFG in context-sensitive ways (Black et al., 1992) or have augmented the formalism with lexical headwords (Magerman, 1995; Collins, 1996).

In this paper, we present a flexible probabilistic parser that simultancously assigns both part-ofspeech tags and a bare-bones dependency structure (illustrated in Figure 1). 'The choice of a simple syntactic structure is deliberate: we would like to ask some basic questions about where lexical relationships appear and how best to exploit

[^0]

Figure 1: (a.) A bare-bones dependency parse, Wach word points to a single parent, the word it modifies; the head of the sentence points to the EOS (end-ofsentence) mark. Crossing links and cycles are not allowed. (b) Constituent structure and subcategorization may be highlighted by displaying the same dependencies as a lexical tree.
them. It is uscful to look into these basic questions before trying to finc-tiune the performance of systems whose behavior is harder to understand. ${ }^{1}$

The main contribution of the work is to propose three distinct, lexicalist hypotheses about the probability space underlying sentence structure. We illustrate how each hypothesis is expressed in a dependency framework, and how cach can be used to guide our parser toward its favored solution. Finally, we point to experimental results that compare the three hypotheses' parsing porformance on sentences from the Wall Street Journal. The parser is trained on an annotated corpus; no hand-written grammar is required.

## 2 Probabilistic Dependencies

It cannot be emphasized too strongly that a grammatical representation (dependency parses, tag sequences, phrasc-structure trees) docs not entail any particular probability model. In principle, one could model the distribution of dependency parses

[^1]in any number of sensible or perverse ways. The choice of the right model is not a priori obvious.

One way to build a probabilistic grammar is to specify what sequences of moves (such as shift and reduce) a parser is likely to make. It is reasomable to expect a given move to be correct about as often on test data as on training data. This is the philosophy behind stochastic CEC (Jelinck et al.1992), "history-based" phrase-structure parsing (Black et al., 1992), and others.

However, probability models derived from parsers sometimos focus on iacidental properties of the data. This may be the case for (Lafferty et al., 1992)'s model for link grammar. If we were to adapt their top-down stochastic parsing strategy to the rather similar case of dependency grammar, we would find their clementary probabilities tabulating only non-intuitive aspects of the parse structure:
$\operatorname{Pr}$ (word $j$ is the rightmost pre-k child of word $i$ $\mid i$ is a right-spine strict descendant of one of the left children of a token of word $k$, or clse $i$ is the
parent of $k$, and $i$ precedes $j$ precedes $k$ ). ${ }^{2}$
While it is clearly necessary to decide whether $j$ is a child of $i$, couditioning that decision as above may not reduce its test entropy as much as a more linguistically perspicuous condition would.

We belicve it is fruitful to design probability models independently of the parser. In this section, we will outline the three lexicalist, linguistically perspicuous, qualitatively different models that we have developed and tested.

### 2.1 Model A: Bigram lexical affinitios

$N$-graun taggers like (Church, 1988; Jolinek 1985; Kupiec 1992; Merialdo 1990) take the following view of how a tagged sentence enters the world. First, a sequence of tags is generated according to a Markov process, with the random choice of each tag conditioned on the previous two tiags. Second, a word is chosen conditional on each tag.
Since our sentences have links as well as tags and words, suppose that after the words are inserted, cach sentence passes through a third step that looks at each pair of words and randomly decides whether to link them. For the resulting sentences to resemble real corpora, the probability that word $j$ gets linked to word $i$ should be lerically sensitive: it should depend on the (tag, word) pairs at both $i$ and $j$.
'The probability of drawing a given parsed sentence from the population may then be expressed

[^2]

Figure 3: (a) The correct parse. (b) 1 common error if the model ignores arity.
as (1) in Figure 2, where the random variable $l_{i j} \in\{0,1\}$ is 1 iff word $i$ is the parent of word $j$.

Dxpression (1) assigns a probability to every possible tag-and-link-amotated string, and these probabilities sum to one. Many of the amotated strings exhibit violations such as crossing links and multiple parents which, if they were allowed, would let all the words express their lexical preferences independently and simultaneously. We stipulate that the model discards from the population any illegal structures that it gencrates; they do not appear in cither training or test data. 'Therefore, the parser described below finds the likeliest legal structure: it maximizes the lexical preferences of (1) within the fow hard limguistic constraints imposed by the dependency formalism.

In practice, some generalization or "coarsening" of the conditional probabilities in (1) helps to avoid the effects of undertraining. For example, we follow standard practice (Church, 1988) in $n$-gram tagging by using (3) to approximate the first term in (2). Decisions about how much coarsconing to do are of great practical interest, but they depend on the training corpus and may be omitted from a conceptial discussion of the model.

The model in (1) can be improved; it does not. capture the fact that words have arities. For example, the price of the slock fell (rigure 3a) will typically be misanalyzed under this model. Since stocks often fall, stock has a greater altinity for fell than for of. Hence stock (as well as price) will end up pointing to the verb fell (Figure 3b), resulting in a double subject for fell and leaving of childless. To capture word arities and other subeategori\%ation facts, we must recognize that the chiddren of a word like fell are not independent of each ot her.

The solution is to modify (1) slightly, further conditioning $L_{i j}$ on the number and/or type of children of $i$ that already sit between $i$ and $j$. This means that in the parse of Figure 3 b, the link price $\rightarrow$ fell will be sensitive to the fact that fellalready has a closer child tagged as a noun (NN). Specifically, the price $\rightarrow$ fell link will now be strongly disfavored in figure 3l, since verbs rarely take two NN dependents to the left. By contrast, price $\rightarrow$ fell is unobjectionable in ligure 3a, rendering that parse more probable. (This change can be reflected in the conceptual model, by stating that the $l_{i j}$ decisions are mado in increasing order of link length $|i-j|$ and are no longer independent.)

### 2.2 Model B: Selectional preferences

In a legal dependency parse, every word except for the head of the sentence (the EOS mark) has

$$
\begin{align*}
& \operatorname{Pr}(\underline{\text { words, tags, links })}=\operatorname{Pr}(\text { words, tags }) \cdot \operatorname{Pr}(\text { link presences and absences } \mid \text { words, tags })  \tag{1}\\
& \approx \prod_{1 \leq i \leq n} \operatorname{Pr}(t w o r d(i) \mid t \operatorname{word}(i+1), t \operatorname{word}(i+2)) \cdot \prod_{1 \leq i, j \leq n} \operatorname{Pr}\left(L_{i j} \mid t \operatorname{tword}(i), t w o r d(j)\right) \\
& \operatorname{Pr}(\operatorname{tword}(i) \mid t \operatorname{word}(i+1), \operatorname{tword}(i+2)) \approx \operatorname{Pr}(\operatorname{tag}(i) \mid \operatorname{tag}(i+1), \operatorname{tag}(i+2)) \cdot \operatorname{Pr}(\operatorname{word}(i) \mid \operatorname{tag}(i))  \tag{3}\\
& \operatorname{Pr}(\underline{\text { words, tags, links }) \propto \operatorname{Pr}(\text { words, tags, preferences })=\operatorname{Pr}(\text { words, tags }) \cdot \operatorname{Pr}(\text { preferences } \mid \text { words, tags }) ~}  \tag{4}\\
& \approx \prod_{1 \leq i \leq n} \operatorname{Pr}(t \operatorname{word}(i) \mid t \operatorname{word}(i+1), t \operatorname{word}(i+2)) \cdot \prod_{1 \leq i \leq n} \operatorname{Pr}(\operatorname{prefcrcnces}(i) \mid \operatorname{tword}(i)) \\
& \operatorname{Pr}\left(\underline{\text { words, tags, links })}=\prod_{1 \leq i \leq n}\binom{1+\# \operatorname{right}-\operatorname{kids}(i)}{\prod_{c=-(1+\# \operatorname{left}-\operatorname{kids}(i)), c \neq 0} \operatorname{Pr}\left(\operatorname{word}\left(\operatorname{kid}_{c}(i)\right) \mid \underset{\substack{\operatorname{tag}\left(\operatorname{kid}_{c-1}(i) \\
\text { or } k i d_{c+1} \text { if } c<0\right.}}{ }\right), \operatorname{tword}(i)}\right. \tag{5}
\end{align*}
$$

Figure 2: High-level views of model $\Lambda$ (formulas 1-3); model B (formula 4); and model C (formula 5). If $i$ and $j$ are tokens, then tword $(i)$ represents the pair $(\operatorname{tag}(i)$, $\operatorname{word}(i))$, and $L_{i j} \in\{0,1\}$ is 1 iff $i$ is the parcut of $j$.
exactly one parent. Rather than having the model select a subset of the $n^{2}$ possible links, as in model $\Lambda$, and then discard the result unless each word has exactly one parent, we might restrict the model to picking out one parent per word to begin with. Model 13 generates a sequence of tagged words, then specifies a parent-or more precisely, a type of parent--for cach word $j$.

Of course model $\Lambda$ also ends up selecting a parent for each word, but its calculation plays careful politics with the set of other words that happen to appear in the sentence: word $j$ considers both the benefit of selecting $i$ as a parent, and the costs of spurning all the other possible parents $i^{\prime}$. Model 13 takes an approach at the opposite extreme, and simply has each word blindly describe its ideal parent. For example, price in l'igure 3 might insist (with some probability) that it "depend on a verb to my right." To capture arity, words probabilistically specify their ideal children as well: fell is highly likely to want only one noun to its left. The form and coarseness of such specifications is a parameter of the model.

When a word stochastically chooses one set of requirements on its parents and children, it is choosing what a link grammarian would call a disjunct (set of selectional preferences) for the word. We may thus imagine generating a Markov scquence of tagged words as before, and then independently "sense tagging" each word with a disjunct. ${ }^{3}$ Choosing all the disjuncts does not quite specify a parse. However, if the disjuncts are sufficiently specific, it specifies at most one parse. Some sentences generated in this way are illegal because their disjuncts cannot bo simultaneously satisfied; as in model $A$, these sentences are said to be removed from the population, and the probabilities renormalized. A likely parse is therefore one that allows a likely and consistent

[^3]set of sense tags; its probability in the population is given in (1).

### 2.3 Model C: Recursive generation

The final model we propose is a generation model, as opposed to the comprehension models $\Lambda$ and 13 (and to other comprehension models such as (Lafferty et al., 1992; Magerman, 1995; Collins, 1996)). The contrast recalls an old debate over spoken language, as to whether its properties are driven by hearers' acoustic needs (comprehension) or speakers' articulatory needs (generation). Models A and B suggest that speakers produce text in such a way that the grammatical relations can be easily decoded by a listener, given words' preferences to associate with cach other and tags' proferences to follow each other. But model C says that speakers' primary goal is to flesh out the syntactic and conceptual structure for each word they utter, surrounding it with arguments, modifiers, and function words as appropriate. According to model C, speakers should not hesitate to add extra prepositional phrases to a noun, even if this lengthens some links that are ordinarily short, or leads to tagging or attachment ambiguities.

The generation process is straightforward. Each time a word $i$ is added, it generates a Markov sequence of (tag, word) pairs to serve as its left children, and an separate sequence of (tag, word) pairs as its right children. Each Markov process, whose probabilities depend on the word $i$ and its tag, begins in a special SIART state; the symbols it generates are added as $i$ 's children, from closest to farthest, until it reaches the STOP state. The process recurses for each child so generated. This is a sort of Iexicalized context-free model.

Suppose that the Markov process, when generating a child, remembers just the tag of the child's most recently generated sister, if any. Then the probability of drawing a given parse from the population is (5), where $\operatorname{kid}(i, c)$ denotes the $c$ thclosest right child of word $i$, and where $\operatorname{kid}(i, 0)=$ STAR'I and kid $(i, 1+\#$ right-kids $(i))=$ STOP.
(a)

(b)


Figure 4: Spans participating in the correct parse of That dachshund over thewe can really play golf!. (a) has one parentless cndword; its subsipan (b) has two.
$(c<0$ indexes left children.) This may be thought of as a non-linear trigram model, where cach tagged word is gencrated based on the parent tagged word and a sister tag. 'The links in the parse serve to pick out the relevant trigrans, and are chosen to get trigrams that optimize the global tagging. 'That the links also happen to anotate useful semantice relations is, from this perspective, quite accidental.

Note that the revised version of model A uses. probabilities Pr(link to child | child, parent, closer-childreu), where model (: uses Ir (link to child | parent, closerechildren). This is because model $\Lambda$ assmoss that the child was previonsly generated by a linear process, and all that is necessary is to link to it. Model C, actually generates the chitd in the process of linking to it.

## 3 Bottom-Up Dependency Parsing

In this section we sketell our dependency parsing atgorithm: a novel dynamic programming method to assemble the most probable parse from the bottom up. The algorithom adds one link at a time, making it easy to multiply ont the models' probability factors. It also enforces the special direc tionality requirements of dependency grammar, the prolitbitions on cycles and multiple parents. ${ }^{4}$

The method used is similar to the CKY method of context-free parsing, which combines analyses of shorter substrings into analyses of progressively longer ones. Multiple analyses have the same signature if they are indistinguishable in their ability to combine with other analyses; if so, the parser discards all but the highest-scoring one. CKY requires $O\left(n^{3} s^{2}\right)$ time and $O\left(n^{2} s\right)$ space, where $n$ is the length of the sentence and $s$ is ant upper bound on signatures per substring.

Let us consider dependency parsing in this framework. One might guess that cach substring analysis should be a lexical tree a tagged headword plus all lexical subtrees dependent upon it. (See Figure 1b.) However, if a constituent's

[^4]

Figure 5: The assembly of a span efrom two smaller spans ( $a$ and $b$ ) and a covering link. Only $a$ is minimal.
probabilistic behavior depends on its beadword the lexicalist hypothesis then differently headed analyses need different sigmatures. There are at least $k$ of these for a substring of length $k$, whence the bound $s:=k=\Omega(n)$, giving a time complex. ity of $\Omega\left(n^{5}\right)$. (Collius, 1996 ) uses this $\Omega\left(n^{5}\right)$ algo. rithon directly (together with pruning).
We propose an altermative approach that preserves the $O\left(u^{3}\right)$ bound. Instead of analyzing sub. strings as lexical trees that will be linked together into larger lexical trees, the parser will analye them as non-constituent spans that will be concatenated into larger spans. $A$ span consists of $\geq 2$ adjacent, words; tags for all these words ex. cept possibly the last; a list of all dependency links among the words in the span; and pertapes some other information carried along in the span's sig mature. No cycles, multiple parents, or crossing links are allowed in tho span, and oach internal word of the span must have a parent in the span.
'Two spans are illustrated in Figure 1 . 'These diagrants are typical: a span of a dependency parse may consist, of either a parentless endword and some of its descendants on one side (F゙igure 4a), or two parentless endwords, with all the right deseendants of one and all the left descendants of the other (Figure 4b). The intuition is that the internal part of a span is grammatically incrt: except for the endwords dachshund and play, the structure of each span is irrelevant too the span's ability to combine in future, so spans with different internal structure can compete to be the best-scoring span with a particular signature.

If span a ends on the same word $i$ that starts span $b$, then the parser tries to combine the two spans by covered-concatenation (frigure 5). 'The two copies of word $i$ are identified, after which a leftward or rightward covering link is optionally added between the endwords of the new span. Any dependency parse can be built up by covered-concatenation. When the parser coveredconcatenates $a$ and $b$, it oltains up to theee new spans (leftward, rightward, and no covering link).

The covered-concatenation of $a$ and $b$, forming $c$, is barred unless it meets certain simple tests:

- a must be minimal (not, itself expressible as a concatenation of narrower spans). This prevents us from assembling $c$ in multiple ways.
- Since the overlapping word will be internal to $c$, it must have a parent in exactly one of $a$ and $b$.

$$
\begin{align*}
& \prod_{k \leq i<\ell} \operatorname{Pr}(t w o r d(i) \mid t w o r d(i+1), t w o r d(i+2)) \cdot \prod_{k \leq i, j \leq \ell \text { with } i, j \text { linked }} \operatorname{Pr}(i \text { has prefs that } j \text { satisfies } \mid \text { tword }(i), \text { tword }(j))  \tag{6}\\
& \prod_{k \leq i, j \leq \ell \text { with } i, j \text { linked }} \operatorname{Pr}\left(L_{i j} \mid t w o r d(i), \text { tword }(j), \operatorname{tag}(\text { next-closest-kid }(i))\right) \cdot \prod_{k<i<\ell,(j<k \text { or } \ell<j)} \operatorname{Pr}\left(L_{i j} \mid t w o r d(i), \text { tword }(j), \cdots\right) \tag{7}
\end{align*}
$$

- $c$ must not be given a covering link if either the leftmost word of $a$ or the rightmost word of $b$ has a parent. (Violating this condition leads to either multiple parents or link cycles.)

Any sufficiently wide span whose left endword has a parent is a legal parse, rooted at the EOS mark (Figure 1). Note that a span's signature must specify whether its cndwords have parents.

## 4 Bottom-Up Probabilities

Is this one parser really compatible with all three probability models? Yes, but for each model, we must provide a way to keep track of probabilities as we parse. Bear in mind that models $\Lambda, B$, and C do not themselves specify probabilities for all spans; intrinsically they give only probabilities for sentences

Model C. Define each span's score to be the product of all probabilities of links within the span. (The link to $i$ from its $c$ th child is associated with the probability $\operatorname{Pr}(\ldots)$ in (5).) When spans $a$ and $b$ are combined and one more link is added, it is casy to compute the resulting span's score: score $(a) \cdot$ score $(b) \cdot \operatorname{Pr}\left(\right.$ covering link). ${ }^{5}$

When a span constitutes a parse of the whole input sentence, its score as just computed proves to be the parse probability, conditional on the tree root EOS, under model C. The highest-probability parse can therefore be built by dynamic programming, where we build and retain the highestscoring span of each signature

Model B. Taking the Markov process to generate (tag, word) pairs from right to left, we let (6) define the score of a span from word $k$ to word $\ell$. The first product encodes the Markovian probability that the (tag, word) pairs $k$ through $\ell-1$ are as claimed by the span, conditional on the appearance of specific (tag,word) pairs at $\ell, \ell+1 .{ }^{6}$ Again, scores can be easily updated when spans combine, and the probability of a complete parse $P$, divided by the total probability of all parses that succeed in satisfying lexical preferences, is just $P$ 's score.

Model A. Finally, model $A$ is scored the same as model B, except for the second factor in (6),

[^5]|  | A | B | C | C | X | Basel |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
| All tokn | $90 . \overline{2}$ | 90.9 | 90.8 | 90.5 | $\mathbf{9 1 . 0}$ | 79.8 |
| Non-punc | 88.9 | 89.8 | $\mathbf{8 9 . 6}$ | 89.3 | $\mathbf{8 9 . 8}$ | 77.1 |
| Nouns | 90.1 | 89.8 | 90.2 | 90.4 | 90.0 | 86.2 |
| Sex verbs | 74.6 | 75.9 | 73.3 | 75.8 | 73.3 | 67.5 |

Table 1: Results of preliminary experiments: Percentage of tokens correctly tagged by each model.
which is replaced by the less obvious expression in (7). As usual, scores can be constructed from the bottom up (though tword $(j)$ in the second factor of (7) is not available to the algorithm, $j$ being outside the span, so we back off to word $(j)$ ).

## 5 Empirical Comparison

We have undertaken a careful study to compare these models' success at generalizing from training data to test data. Full results on a moderate corpus of $25,000+$ tagged, dependency-annotated Wall Street Journal sentences, discussed in (Eisner, 1996), were not complete at press time. However, 'Tables 1-2 show pilot results for a small set of data drawn from that, corpus. (The full results show substantially better performance, e.g., $93 \%$ correct tags and $87 \%$ correct parents for model C , but appear qualitatively similar.)
'The pilot experiment was conducted on a subset, of 4772 of the sentences comprising 93,360 words and punctuation marks. The corpus was derived by semi-automatic means from the Penn Treebank; only sentences without conjunction were available (mean length $=20$, max $=68$ ). $\Lambda$ randomly selected set of 400 sentences was set aside for testing all models; the rest were used to estimate the model paramcters. In the pilot (unlike the full experiment), the parser was instructed to "back off" from all probabilities with denominators $<10$. For this reason, the models were insensitive to most lexical distinctions.

In addition to models $\Lambda, B$, and $C$, described above, the pilot experiment evaluated two other models for comparison. Model $\mathrm{C}^{\prime}$ was a version of model C that ignored lexical dependencies between parents and children, considering only dependencies between a parent's tag and a child's tag. This model is similar to the model used by stochastic CFG. Model X did the same $n$-gram tagging as models $\Lambda$ and B ( $n=2$ for the preliminary experiment, rather than $n=3$ ), but did not assign any links.
Tables 1-2 show the percentage of raw tokens that were correctly tagged by each model, as well as the proportion that were correctly attached to

|  | A | 13 | (; | C' | Baseline |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\overline{\text { All tokens }}$ | 75.9 | 72.8 | 78.1 | 66.6 | 47.3 |
| Nou-Intunc | 75.0 | 75.4 | 79.2 | 68.8 | 51.1 |
| Nouns | 75.7 | $7 \mathrm{~T} . \overline{8}$ | 77.2 | 55.9 | 29.8 |
| Lexical verbs | 66.5 | 63.1 | 71.0 | 46.9 | 21.0 |

Table 2: Results of preliminary experiments: Per. contage of tokens correctly attached to their parents by cach model.
their parents. Nor tagging, baseline performance was measured by assigning each word in the test set its most frequent tag (if any) from the training set. The ummally low baseline performance results from a combination of a sinall pilot training set and a mildly extended tag set." We ob-. served that in the training set, determiners most commonly pointed to the following word, so as a parsing baseline, we linked every test determiner to the following word; likewise, we linked every test preposition to the preceding word, and so on.

The patierns in the preliminary data are striking, with verbs showing up as an area of difficulty, and with some models clearly faring better than other. 'The simplest and lastest model, the recursive generation model $C$, did easily the best job of capturing the dependency structure ('Lable 2). It misattached the fewest words, both overall and in each category. This suggests that subcategorization preferences - the only factor considered by model C play a substantial role in the structure of Treebank sentences. (Indeed, the errors in model B, which performed worst across the board, were very frequently arity errors, where the desire of a child to attach to a particular parent overcame the reluctance of the parent to acept more children.)

A good deal of the parsing success of model (, scems to have arisen from its knowledge of individual words, as we expected. 'This is shown by the vastly inferior performance of the control, model (U'. On the other hand, both C, and C' were competitive with the other models at tagging. 'This shows that a tag can be predicted about as well from the tags of its putative parent and sibling as it can from the tag's of string-adjacent words, even when there is considerable error in determining the parent and sibling.

## 6 Conclusions

Bare-bones dependency grammar - which requires no link labols, no grammar, and no fuss to understand -is a clean testbed for studying the lexical alfinities of words. We believe that this is an important line of investigative research, one that is likely to produce both useful parsing tools and significaut insights about language modeling.

[^6]As a first step in the study of lexical affin. ity, we asked whether there was a "natural" way to stochasticize such a simple formalism as dependency. In fact, we have now exhibited three promising lypes of model for this simple problem. Further, we have developed a novel parsing algorithm to compare these hypotheses, with results that so far favor the speaker-oriented model C, even in written, edited Wall Street Journal text. 'To our knowledge, the relative merits of speakeroriented versus hearer-oriented probabilistic syntax models have not been investigated before.

## References

Fiara Black, Fred , Felinek, et al. 1992. Towards historybassed grammars: using richer models for probabilistic parsing. In liflh DARPA Workshop on Speech and Natural Language, Arden Conference Center, Harriman, New York, lebenary.
Kenneth W. Church. 1988. A stochastic parts program and nonn phrase parser for mestricked text. In Proc, of the end Conf. on Applied Natural Language Processing, 136-148, Nustim, 'TX. Association for Computational linguistics, Morristown, NJ.
Michacl J. Collins. 1996. A new statistical parsee based on bigram lexical dependencies. In froceedings of the 3 the $A C I$, Santia Cruz, CA, July.
Jason lisner. 1996. An empirical comparison of prob ability models for clependency grammar. 'Techmical Report IRCS-96-11, University of Pennsylvania.
Fred Jelinek. 1985. Markov source modeling of text generation. In A. Skwirainski, oditor, Impact of Processing Techniques on Commamicalion, Dordrecht.
Fired Jolinek, John D. Lafferty, and Robert L. Merees. 1992. Basic: methods of probabilistic context-free grammars. In Speech Recognition and Understanting: Recent Advances, Trends, and Applications.
J. Kupiec. 1992. Robust part-of-speech tagging using a hidden Markov model. Gompuler Speech and hanguage, 6.
John Lafferty, Daniel Sleator, and Davy Temperley. 1992. Grammatical trigrams: A probabilistic: model of link grammar In Proce of the AAAI Conf. on Probabilistic Approaches to Natural language, Oct.
David Magerman. 1995. Statistical decision-tree models for parsing. In Procectings of the 33 rd Annual Meeting of the $A C L$, Boston, MA.
Igor A. Mel'čak. 1988. Dependency Syntax: Theory and Practice. State University of New York Press.
13. Merialdo. 1990. 'Tagging text with a probabilistic: model. In Proceedings of the IBM Natural Language TTh, laris, l'rance, pp. 161-172.

Yvos Schabes. 1992. Stochastic lexicalized treeadjoining grammars. In Procecdings of COITNG92, Nantes, France, July.
Daniel Sleator and Davy Temperley. 1991. Parsing Finglish with a link Crammar. Technical report OMU..CS-91-196. CS Dept., Garnegie Mellon Univ.


[^0]:    *'l'his material is based upon work supported under a National Science Fonndation Graduate Fellowship, and has benefited greatly from discussions with Mike Collins, Dan Melamed, Mitch Marcus and Adwait Ratnaparkhi.

[^1]:    ${ }^{1}$ Onr novel parsing algorithm also rescues dependency from certain criticisms: "Dependency grammars ... are not lexical, and (as far as we know) lack a parsing algorithm of eflicicncy comparable to link grammars." (Lafferty et al., 1992, p. 3)

[^2]:    ${ }^{2}$ This corresponds to lafferty et al.'s central statistic (p. 4), $\operatorname{Pr}(W, \leftarrow-\mid I, R, l, r)$, in the case where $i$ 's parent is to the left of $i$. $i, j, k$ correspond to $J, W, R$ respectively. Owing to the particular recursive stratcgy the parser uses to break up the sentence, the statistic would be measured and utilized only under the condition described above.

[^3]:    ${ }^{3}$ In our implementation, the distribution over possible disjuncts is given by a pair of Markov processes, as in model C .

[^4]:    ${ }^{4}$ Tabeled dependencies are possible, and a minor variant handles the simpler case of link grammar. Indeed, abstractly, the algorithm resembles a deaner, bottom-up version of the top-down link grammar parser developed independently by (Lafferty et al., 1992).

[^5]:    ${ }^{5}$ The third factor depends on, e.g., $\operatorname{kid}(i, c-1)$, which we recover from the span signature. Also, matters are complicated slightly by the probabilities associated with the generation of STOP.
    ${ }^{6}$ Different $k-\ell$ spans have scores conditioned on different hypotheses about $\operatorname{tag}(\ell)$ and $\operatorname{tag}(\ell+1)$; their signatures are correspondingly different. Under model $B$, a $k-\ell$ span may not combine with an $\ell-m$ span whose tags violate its assumptions about $\ell$ and $\ell+1$.

[^6]:    ${ }^{7}$ We used distinctive tags for auxiliary verbs and for words being used as nomm modifiess (o.g., participles), because they have very different subcategorization frames.

