# Disambiguation by Prioritized Circumscription 

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#### Abstract

This paper presents a method of resolving ambiguity by using a variant of circumseription, prioritized circumseription. In a disambiguation task, human seens to use various preferences which have varions strength. In prioritized cir cumscription, we can express these preferences as defeasible constraints with various strength and we infer the most preferable logical models which satisfy stronger constraints as much as possible. This representation is very natural for disambiguation since we can regard a logical interpretation as a possible reading athd the most preferable logical models as the most preferable readings. We argue that prioritized circumseription is another promising method for the task. We also discuss an inplementation of prioritized circhmseription by a hierarchical logic programming (HCLD) language.


## 1 Introduction

This paper presents a method of disambiguation task by a variant of circumscription, prioritized circumscription (McCarthy, 1986; Lifschil/z, 1985) and discnss its implementation by a hierarchical constraint logic programming (HCLP) language such as (Borning et al., 1989).

Disambiguation is a very important task in natural language processing. To resolve anbiguity, humanss sem to use not only syntactic constraints but also varions levels of heuristics such as grammatical preferences (Hobbs, 1990) and semantic preferences; (Wilks, 1975).

For example, suppose that we have the following sentences.

John just saw a man with a telescope. (a)
He bought the telescope yesterday.
Although there is an ambiguity on meaning of the phrase. "with a telescope" (the telescope is either
used by John or carried by the man), we might conclude the preferred reading as follows.

F'rom the above sentences, "He" would be equal to John because the subject tends to be continned to the next sentence and John probably had a telescope at the time of seeing a man from the sentence (b) aud inertia of possession. Therefore, from this preferred reading, we conclude that the telescope is used as a device to see a man.

However, this reading is not final since at least the following preferences are involved in the above reading and these preferences can be defeated by stronger information.
Syntactic preference: The subject tends to be continued.
Semantic preference: If a person buys something at, time $i$, then he should have it at time $j$ where $i<j$.
In order to demonstrate defeasibility of preference rules, suppose the following sentence is added after the above sentences (a) and (b).

But, he gave the man the telescope (c)
this morning.
Then, we might change a preferred reading that the man shonld have had a telescope and therefore, the telescope was carried by the man at the time of John's seeing the man. In this reading, at least, the following preference rule of another inertia of possession is used.

If a person gives something to the other
person at time $i$, then the other person should have it at time $j$ where $i<j$.
This conflicts with the former semantic preference of incrtia of possession by buying, but the above preference is stronger than the former since the time of giving is later than the time of buying. Thus, the former preference becomes no loner applicable by the new sentence.

This kind of revision of reading cannot be represented by inference in classical logic since in classical logic, once we get a inferred result, we can no longer retract the result ( monotonic: property). 'lherefore, to understand the phenomena, we noed other reasoning methods and in fact,
many researches have been using general reasoning fyameworks in Artificial Intelligence such as abduction (Hobbs et al.. 1993), prol)abilistic network (Charniak and Goldman, 1989), truth maintenance system (Zernik and Brown, 1988), default logic (Quantz, 1993) and conditional logic: (Lascarides. 1993). In this paper, we propose another alternative, that is, circumscription (McCarthy, 1986: Lifschit\%, 1985). Even though circumseription is one of the most popular formalisms in the commmity of nommonotonic reasoning research, it is surprising that very fow has examined feasibility of circumscription for disambiguation. Our work of disambiguation by interpretation ordering is originated from (Satoh, 1991) and in a more recent work, Kameyama (Kameyama, 1994) has indepemdently proposed usage of circumscription for interpretation of pronominal anaphora.

In this paper, we explore this direction further. In circumscription, we give a preference order over logical interpretations and consider the most preferable models. This representation naturally corresponds with a disambiguation task since we can regard a logical interpretation as a possible reading, and disambiguation as a task to get the most preferable reading among possible readings. Among variants of circumseription, prioritized circumscription is suitable to represent various strength of preference rules. In prioritized circumseription, we can divide preference rules into hierarchy and this hierarchy gives a priority relation over preferences. Therefore, we directly represent rules in the hiemarchy in prioritized circumscription.

We believe that circumscription has the following advantages in the task of resolving ambignity.

- Since we use a first-order predicate calculus for a basic language, we can represent varions kinds of information such as grammatical rules and semantical rules in one framework.
- There is ouly one extra underlying mechanism besides inference rules for the first-order predicate calculus, that is, introducing an order over logical interpretations. Therefore, reasoning process can be utuderstood casily compared to other mechanism using ummerical reasoning or complex inference rules.
- We do not need to assign detailed numerical valnes to preference rules in order to express priority over preference rules, but just specify a preference level of the rules. This representation can be regarded as an assignment of qualitative strength for preference rules and reduces a burden of representing a priority over preference rules greatly. Moreover, this prioritization is general since we can represent a various kind of priority besides specificity.
- It is important to retain possible readings if we can not. resolve ambiguity yot. In circumscription, we can consider multiple preferable models,
not necessary the single preferable model. So. if there are yet multiple possible readings as a result of disambiguation, we can keep these possible readings as multiple preferable morlels.

In this paper, we also discuss an implementation by using hierarchical constraint logic programming (HCLP) language such as (Borning et al., 1989). HCLP language is similar to constraint logic programming language except that we can represent a constraint hierarchy. Thus, there is a correspondence between a solution of an HCLP language and the most preferable models of prioritized circumscription. In this paper, we use our HCL $P$ language based on a boolean constraint solver to get the most preferable models from preference rules represented as boolean constraints in the HCLI language. We demonstrate how the above example of the disambiguation is treated in the HCLP langnage.

## 2 Prioritized Circumscription

In this section, we briefly review prioritized circumscription. For simplicity sake, we morlify the definition of prioritized circumscription by (McCarthy, 1986; Lifschitz, 1985). The difference is that we let all predicates vary and maximize preference rules whereas Lifschitz minimize abnormal predicates for preference rules.

Let, $\Phi(\mathbf{x})$ and $\Psi(\mathbf{x})$ be formnlas with the same number of free variables $\mathbf{x}$. We say that $\Phi$ and $\Psi$ are similar. $\Phi \geq \Psi$ stands for $\forall \mathbf{x}(\Psi(\mathbf{x}) \supset \Phi(\mathbf{x}))$. We extend this notation to tuples of formulas $\Phi, \Psi$ where $\Phi=\Phi_{1}, ., \Phi_{n}$ and $\Psi=\Psi_{1}, \ldots, \Psi_{n}$ and $\Phi$ and $\Psi$ are similar (each $\Phi_{j}$ and $\Psi_{j}$ are similar): $\Phi \geq \Psi$ stauds for $\wedge_{j=1}^{n /} \Phi_{j} \geq \Psi_{j}$. We also write $\Phi \geq \Psi \wedge \Psi \geq \Phi$ as $\Phi=\Psi$ and $\Phi \geq \Psi \wedge \neg(\Psi \geq \Phi)$ as $\Phi>\Psi$.

Let a tuple of formulas $\Phi$ be broken into disjoint parts $\Phi^{1}, \Phi^{2}, \ldots, \Phi^{k}$. Let $\Psi^{i}$ be similar to $\Phi^{i}$. We define $\Phi \succeq \Psi \stackrel{\text { def }}{=} \wedge_{i=1}^{k}\left(\wedge_{j=1}^{i \cdots 1} \Phi^{j}=\Psi^{j} \supset \Phi^{i} \geq \Psi^{i}\right)$. We also write $\Phi \succeq \Psi \wedge \neg(\Psi \succeq \Phi)$ as $\Phi \succ \Psi$.

Definition 1 Let $A(\mathbf{P})$ be a formula and $\Phi(\mathbf{P})$ be a tuple of formiulas which is broken into $\Phi^{1}(\mathbf{P}), \Phi^{2}(\mathbf{P}), \ldots, \Phi^{k}(\mathbf{P})$ where $\mathbf{P}$ is a tuple of predicates used in these formulas.

The symtactic definition of prioritized circumscription is as follous:

$$
\begin{equation*}
A(\mathbf{P}) \wedge \neg \exists \mathbf{p}(A(\mathbf{p}) \wedge \Phi(\mathbf{p}) \succ \Phi(\mathbf{P})) \tag{1}
\end{equation*}
$$

where

1. p is a tuple of predicate variables each of which has the same arity as the corresponding predicate constant in $\mathbf{P}$,
2. $A(\mathbf{p})(\Phi(\mathbf{p}))$ is a formula obtained by replacing every occurrence in $A(\Phi$, respectively) of a predicate constant in $\mathbf{P}$ by the corresponding predicate variable in $\mathbf{p}$.

According to the result of (Lifschitz, 1985), we give a model theoretic definition of the above formula (1) as follows.
Definition 2 We define an order $\geq$ oner logical interprelations.s ass follours:

$$
M^{\prime} \geq M
$$

where

1. $M^{\prime}$ and $M$ have the same domain.
2. certy constant and function symbol hats the same intcrpretation in $M^{\prime}$ and $M$.
3. $\Phi(\mathrm{p}) \leftrightharpoons \Phi(\mathrm{q})$ is true in. $M^{\prime}$ (or. cquimatently. in $M$ ) for $M^{\prime}[\mathbf{P}]$ as. $\mathbf{P}$ and $M[\mathbf{P}]$ ass q where $M^{\prime}[\mathbf{P}](M[\mathbf{P}])$ is a tuple of the extensions for $M^{\prime}(M$. respectinely) of predicates in $\mathbf{\Gamma}$
In the above order, a greater interpretation is nore preferable. The above order intuitively means that logical interpretations which maximally satisfy a subset of $\Phi^{1}$ are preferable, and if there are interpretations which satisfy the same formulas in $\Phi^{\prime}$, then interpretations which maximally satisfy a subset of $\Phi^{2}$ are preferable, and... and if there are interpretations which satisfy the same formulas in $\Phi^{k-1}$, then interpretations which maximally satisfy a subset of $\Phi^{k}$ are preferable.

Let $A$ be a formula. We say that a logical interpretation $M$ is the most preferable model in the clas.s of models of $A$ w.r.t. $\geq$ if there is no model $M^{\prime}$ of $A$ in the class such that $M^{\prime} \geq M$ and not $M \geq M^{\prime}$.

According to the result of (Lifschith, 1985), we lave the following correspondence between syutactio defintition and semantic definition.
Theorem 1 A hogical interpretation $M$ is a modet of (1) iff $M$ is the most preferable model w.r.t. $\geq$ in the class of modeles of $A$.

## 3 Disambiguation by Prioritized Circumscription

In order to nse prioritized circumscription for a disambiguation lask, we make the following correspondence between formmas in the definition of prioritized circumscription and information in natural langrage. In the syotactic elelinition of prioritized circtumseription in Section 2, we correspond $A$ with information about given sentences and background knowledge which is atways true in any situation. And, we regard $\Phi$ as a tuple of preference rules. Note that preference rules are put into liectarchy according to strength of preference rules. Then, the most preferable models correspond with the most peferable readings since each model satislies stronger preference rules as much as possible and therefore, the syntactic defintion becomes a specification of the preferable readings by Theorem 1.

In the subseduent subsections, we tirstly fix an experitnental logical representation of sentences, backgrond knowledge and preferences. Then, we

Lreat the example in Section 1 by the logical representation.

### 3.1 Logical Representation of Sentences and Background Knowledge

We use an adaptation of Kowalski's event calculus (Kowalski and Sergot, 1986). However, the idea of disambignation in this paper does not depend on a particular representation. We assume that each sentence expresses an event. For example, a sentence "John gave the telescope to the man" is represented as the following formma.

```
act(l', Cive)^actor(E,John)^
objecl(F,T'elescope) ^ recipient(F, Man)
```

A complex sentence is supposed to be decomposed into a sed of simple sentences which is translated into the above representation. Ambiguities are expressed by disjunctions. For example, the sentence "John saw a man with a telescope" is expressed as follows.

```
fime(L,T')^act(H,Sce)
Aactor(E,John) ^object(L,Man)
^(dovice(b,Tclescope)
    V(time ( }\mp@subsup{F}{}{\prime\prime},T)\wedge\operatorname{act}(\mp@subsup{E}{}{\prime},Have
        ^actor( (',Man)^objcet( }\mp@subsup{E}{}{\prime\prime}, Telescope))
```

The last conjunct expresses ambiguity in the phatase "with a telescope" (used as a device or carried by the man).

In addition to the semantic representation, we also use syntactical information from a parser so that grammatical preference rules can be expressed. For example, we show some of the grammatical information of the sentence "John gave the telescope to the man" as follows. (We assmuce that sentence number is 1).

```
subj(1,Iohn) ^verb(1,Gioe)
Adirect_obj(1,Telescope)
Amditect_obj(1, Man)
A in_the_sentence(1, John)
```

By using these basic predicates, we can represent background knowledge which are always valid. For example, backgromut knowledge "If $a_{1}$ has 0 at time $i_{\text {, and }} a_{1}$ is not equal to $a_{2}$, then $a_{2}$ does not have o at titue $i$ can be expressed in the fol lowing formulal.

```
\foralle\foralli\forall\mp@subsup{a}{1}{}\forall\mp@subsup{a}{2}{}\forallo\forall\mp@subsup{c}{1}{}(
    (timec(c,i) ^act(e, Have) ^actor(e, a, )
    \wedgeobject(c,o)\wedge \negeq(a, (a, (a ) ) \supset
        ((lime (e, , i)\wedge act(e, Have)
        Aaclor(e, c, , (2)) \supset \negobject(c,o,o))
```


### 3.2 Logical Representation of Preferences

We represent a preference rule as a formula in $\Phi$ in The syutactic definitiou of prioritized circumscription and handle a prionity among preferences by

[^0]putting stronger preferences into a stronger hierarchy of preferences.

For example, consider the following two grammatical preferences.

1. If "He" appears in a sentence as the subject and the subject in the previous sentence is male, then it is preferable that "He" refers to the previous subject.
2. If "He" appears in a sentence as the subject and someone in the previous sentence is male, then it is preferable that " $H e$ " refers to the one in the previous sentence.
Suppose that the former is stronger than the latter. This priority of the preferences means that the formula:

$$
\begin{aligned}
& (i \operatorname{san}(a, M a l e) \wedge \operatorname{subj}(i, a) \\
& \quad \wedge \text { in_the_sentence }(i+1, H e)) \supset e q(a, H e)
\end{aligned}
$$

should be satisfied as much as possible for every $a$ and $i$, and if it is maximally satisfied then the following formula:

$$
\begin{aligned}
& (\text { (isa }(a, \text { Male }) \wedge \text { in_the_sentence }(i, a) \\
& \quad \text { in_the_sentence }(i+1, H e)) \supset \operatorname{eq}(a, H e)
\end{aligned}
$$

should be satisfied as much as possible for every $a$ and i.

We can represent semantic preferences as well. For example, a preference "If $a_{1}$ sees $a_{2}$, then $a_{2}$ and $a_{1}$ are not equal" means that the following expression should be satisfied as much as possible for every $e, a_{1}$ and $a_{2}$ :

$$
\begin{align*}
& \left(\operatorname{act}(c, S e e) \wedge \operatorname{actor}\left(e, a_{1}\right) \wedge \operatorname{object}\left(e, a_{2}\right)\right) \supset  \tag{5}\\
& \quad \rightarrow e q\left(a_{2}, a_{1}\right)
\end{align*}
$$

Note that the above is a preference rule because there is a possibility of reflexive use of "see".

### 3.3 Example

Now, we are ready to treat disambiguation of the sentences used in Section 1 by prioritized circumscription.

We consider the following background knowledge which is always true. We denote the conjunctions of the following axioms as $A_{0}(\mathbf{P})$ where
$\mathbf{P} \stackrel{\text { def }}{=}\langle e q$, is, time, act, actor, object, recipient, device, subj, in_the_sentence $\rangle$.

1. If $a_{1}$ is equal to $a_{2}$ then $a_{2}$ is equal to $a_{1}$.

$$
\forall a_{1} \forall a_{2}\left(e q\left(a_{1}, a_{2}\right) \supset e q\left(a_{2}, a_{1}\right)\right)
$$

2. If $a_{1}$ and $a_{2}$ are equal and $a_{2}$ and $a_{3}$ are equal, then $a_{1}$ and $a_{3}$ are equal.

$$
\begin{aligned}
& \forall a_{1} \forall a_{2} \forall a_{3}\left(\left(e q\left(a_{1}, a_{2}\right) \wedge e q\left(a_{2}, a_{3}\right)\right) \supset\right. \\
& \left.\quad e q\left(a_{1}, a_{3}\right)\right)
\end{aligned}
$$

3. If $a_{1}$ is equal to $a_{2}$, then $a_{2}$ is an actor of $a_{1}$ 's action, too.

$$
\begin{aligned}
& \forall e \forall a_{1} \forall a_{2}\left(\left(e q\left(a_{1}, a_{2}\right) \wedge \operatorname{actor}\left(e, a_{1}\right)\right) \supset\right. \\
& \left.\quad \operatorname{actor}\left(e, a_{2}\right)\right)
\end{aligned}
$$

4. If $a$ use $o$ as a device at time $i$ them $a$ has $o$ at time $i$.
```
\(\forall e \forall i \forall a \forall o((t i m e(e, i) \wedge \operatorname{actor}(e, a)\)
    \(\wedge\) device \((e, o)) \supset\)
    \(\exists e_{1}\left(\right.\) time \(\left(e_{1}, i\right) \wedge \operatorname{act}\left(e_{1}, H a v e\right)\)
        \(\left.\left.\wedge \operatorname{actor}\left(e_{1}, a\right) \wedge \operatorname{object}\left(e_{1}, o\right)\right)\right)\)
```

5. If $a_{1}$ has $o$ at time $i$, and $a_{1}$ is not equal to $a_{2}$, then $a_{2}$ does not have $o$ at time $i$.
This is same as (2).
We consider the following preferences.
6. If $a_{1}$ sees $a_{2}$, then $a_{1}$ and $a_{2}$ are not equal.
$\Phi_{1}^{1}\left(\mathbf{P}, e, a_{1}, a_{2}\right)=(5)$
7. If $a$ is male and $a$ is the subject of $i$-th sentence and "He" is in the next sentence, then $a$ is equal to "He".
$\Phi_{1}^{2}(\mathbf{P}, e, a, i)=(3)$
8. If $a$ is male and $a$ is in $i$-th sentence and " $H e$ " is in the next sentence, then $a$ is equal to "He".
$\Phi_{1}^{3}(\mathbf{P}, a, i)=(4)$
9. If someone gives $o$ to $a$ at time $i$, then $a$ has $o$ at time $i+1$. This expresses inertia of ownership.

$$
\begin{aligned}
& \Phi_{1}^{4}(\mathbf{P}, e, a, o, i)= \\
& \quad(\text { act }(e, \text { Give }) \wedge \text { object }(e, o) \\
& \wedge \operatorname{recipient}(e, a) \wedge \operatorname{time}(e, i)) \supset \\
& \quad \exists e_{1}\left(\operatorname{act}\left(e_{1}, H a v e\right) \wedge \operatorname{actor}\left(e_{1}, a\right)\right. \\
& \left.\quad \wedge o b j e c t\left(e_{1}, o\right) \wedge \operatorname{time}\left(e_{1}, i+1\right)\right)
\end{aligned}
$$

5. If $a$ buys $o$ at time $i$, then $a$ has $o$ at time $i+2$. This preference of another inertia of ownership is weaker than the former preference because time interval is longer than the former preference.

$$
\begin{aligned}
& \Phi_{1}^{5}(\mathbf{P}, e, a, o, i)= \\
& \quad(\text { act }(e, B u y) \wedge \operatorname{actor}(e, a) \\
& \wedge o b j e c t(e, o) \wedge \operatorname{time}(e, i)) \supset \\
& \quad \exists e_{1}\left(\operatorname{act}\left(e_{1}, \operatorname{Have}\right) \wedge \operatorname{actor}\left(e_{1}, a\right)\right. \\
& \left.\quad \wedge \operatorname{object}\left(e_{1}, o\right) \wedge \operatorname{time}\left(e_{1}, i+2\right)\right)
\end{aligned}
$$

We assume that $\Phi_{1}^{1}$ is a formula which should be satisfied in the first place, $\Phi_{1}^{2}$ in the second place, $\Phi_{1}^{3}$ in the third place, $\Phi_{1}^{4}$ in the fourth place and $\Phi_{1}^{5}$ in the fifth place.
Example 1 We consider the following sentences. John just saw a man with a telescope. He bought the telescope yesterday.
A logical representation of the above sentences is as follows and we denote it as $A_{1}(\mathbf{P})$.

```
\(\operatorname{time}\left(E_{1}, 2\right) \wedge \operatorname{act}\left(E_{1}, S e e\right) \wedge \operatorname{actor}\left(E_{1}, J o h n\right)\)
^object( \(E_{1}\), Man) \(\wedge i s a(J o h n\), Male \()\)
\(\wedge i s a(M a n, M a l e) \wedge \operatorname{subj}(1, J o h n)\)
Ain_the_sentence ( 1, John)
Ain_the_sentence (1, Man)
\(\wedge\left(\right.\) device \(\left(E_{1}\right.\), Telescope \()\)
    \(\vee\left(\operatorname{actor}\left(E_{1}^{\prime}, \operatorname{Man}\right) \wedge\right.\) time \(\left(E_{1}^{\prime}, 2\right)\)
    \(\wedge \operatorname{act}\left(E_{1}^{\prime}, H a v e\right) \wedge \operatorname{object}\left(E_{1}^{\prime}\right.\), Telescope \(\left.\left.)\right)\right)\)
```

$\wedge t i m e\left(E_{2}, 0\right) \wedge \operatorname{act}\left(E_{2}, B u y\right)$
へactor $\left(L_{2}, H e\right) \wedge$ object $\left(E_{2}\right.$, Telescope $)$
Ain_the_sentence $(2, H e)$
Note that we represent, "just" as time 2 and "yesterday" as time 0.

In the syutactic definition of the most preferable reading (1), we let $\Lambda(\mathbf{P})$ be $A_{0}(\mathbf{P}) \wedge A_{1}(\mathbf{P})$ and $k$ be 5.
We show an intuitive explanation of inference of gettitug the most preferable reading as follows. From the preference 2, "The" preferably refers to John. Note that although the preference 3 seens to be applicable, it is not actually used since the stronger preference 2 overrides the preference 3 .

Then, from the preference 5 , John had the telescope at time 2. From the preference 1, John is not equal to the man. Then, the man cannot have the telescope at time 2 from the background knowledge 5 and therefore, the telescope was used as a device from the disjunction in $A_{1}(\mathbf{P})$. We can actually prove that device ( $L_{1}$, telescope) is true in the most preferable readings.
Example 2 Suppose we add the following sentence to the prewious sentences.

## But, he gave the telescope to the man this morning.

A logical representation related to this sentence is as follows. We denote the formula as $\Lambda_{2}(\mathbf{P})$.

$$
\begin{aligned}
& \operatorname{time}\left(L_{3}, 1\right) \wedge \operatorname{act}\left(E_{3}, \text { Give }\right) \wedge \operatorname{actor}\left(E_{3}, H_{c}\right) \\
& \wedge o b j e c t\left(I_{3}, \text { Telescope }\right) \wedge \operatorname{recipient}\left(E_{3}, M a n\right)
\end{aligned}
$$

Note that we represent "this morning" as time 1.
In this case, we let $A(\mathbf{P})$ be $A_{0}(\mathbf{P}) \wedge A_{1}(\mathbf{P}) \wedge$ $A_{2}(\mathbf{P})$ in the syntactic definition. Then, reading of "with a telescope" is changed. From the preference 4 , the man should have had the telescope at time 2. If the telescope were used as a device at time 2, John would also have the telescope at the same time according to backgronnd knowledge 4 and it contradicts background knowledge 5. Then, the weaker preference 5 is retracted to avoid contradiction and the stronger preference 4 is survived. 'Thorofore, in the most preferable reading, the mant had the telescope at time 2 .

## 4 HCLP language

Now, we discuss an intplementation of prioritived circumscription by HCLP. Firstly, we briefly review a hieratchical constraint logic programming(HCLIP) language. We follow the definition of (Borning et al., 1989).

An HCLP program consists of rules of the form: $h:-b_{1}, \ldots, b_{n}$
where $h$ is a predicate and each of $b_{1}, \ldots, b_{7}$ is a predicate or a constraint or a labeled constraint. A labeled constraint is of the form:

## label $C$

where $C$ is a constraint in specific domain and label is a label which expresses strength of the constraint $C$.

The operational semantics for HCLP is similar to CLI' except manipulating a constraint hierarchy. In HCLP, we accumulate labeled constraints to form a constraint hicrarchy by each label while executing CLP until CLP solves all goals and gives a reduced required constraints. 'Then, we solve constraint hierarchy with required constraints.
'Lo solve constraint hierarchy, we firstly find a maximal subset of constraints for the strongest; level which is consistent with the required constraints. 'Then, we try to find a maximal sulset of constraints in the second strongest level with respect to the umion of the required constraints and the maximal consistent subset for the strongest level,.., and so on until a maximal consistiont subset of constraints in the $k$-th strongest level is added. 'Then, an assignment which satisfies the final set of constraints is called a solution.

Leti $\theta$ and $\sigma$ be assignments and $C_{\theta}^{1}\left(\right.$ and $\left.C_{\sigma}^{1}\right)$ be a set of constraints in the strongest level of the hierarchy satisfied by $\theta($ and $\sigma)$, and $C_{\theta}^{2}($ and $C_{\sigma}^{2}$ ) be a set of constraints in the second strongest level of the hierarchy satisfied by $\theta($ and $\sigma) \ldots$, and $C_{\theta}^{\gamma_{i}}\left(\right.$ and $\left.C_{\sigma}^{k}\right)$ be a set of constraints in the $l_{i-\text { th }}$ strongest level of the hicrarchy satisfied by $\theta$ (and $\sigma$ ).
$\theta$ is locally-predicate-better (Borming et al., 1989) than $\sigma$ w.r.t. the constraint hierarchy if there exists $i(1 \leq i \leq k)$ such that for every $j(1 \leq j \leq i-1), C_{\sigma}^{j}=C_{\theta}^{j}$ and $C_{\sigma}^{i} \subset C_{\theta}^{i}$,

We can prove that if $\theta$ is a solution, then there is no assignment; $\sigma$ which satisfies the required constraints and is bocally-predicate-better than $\theta$.

Note that the definition of locally-predicatebetter comparator is similar to the defintion of the order over logical interpretation in the prioritized circumscription. The difference is that locally-predicatie-better comparator considers assignments for variables in constraints in HCLI' whercas the order over logical interpretation considers assignments of truth-value for formulas in prioritized circumscription.

## 5 Implementation by HCLP language

In order to use HCLP language for implementation of prioritized circumscription, we need to change formulas in prioritized circumscription into constraints in HCLP. It is done as follows. We introduce a domain closure axiom so that we only consider relevant constants used in the given sentences. Then, we instantiate universal-cuantified variables in background knowledge and free variables in preferences with the relevant constants and iutroduce Skolem functions for existentialquantified variables.

For example, we lave the following formula by instantiating preference 4 in Section 3.3 with $F_{3}$ for $e$ and the man for $a$ and the telescope for $o$ and 1 for $i$ and introducing a Skolem function $f$ :
(act $\left(E_{3}\right.$, Give $) \wedge$ object $\left(E_{3}, T e l e s c o p e\right) ~()$
^recipient $\left.\left(E_{3}, \operatorname{Man}\right) \wedge \operatorname{time}\left(E_{3}, 1\right)\right) \supset$
(act $f\left(E_{3}\right.$, Man, Telescope, 1), Have)
Aactor $\left(f\left(E_{3}\right.\right.$, Man. Telescope, 1), Man)
Nobject $f\left(E_{3}\right.$, Man, Telescope, 1). Telescope $)$
$\wedge$ time ( $f\left(E_{3}\right.$, Man, Telescope, 1), 2) )
By this translation, every formula becomes ground and we regard a different ground atom as a different propositional symbol. 'Then, every formula in prioritized circumscription can be regarded as a boolean constraint in HCLP. We translate all formulas in the syntactic definition of the background knowledge and the sentences in Examples 1 and 2 into boolean constraints in our IICLP language (Satoh, 1990). Then, from the two sentences in Example 1, our HCLD language gives the following result as a part of a solution:
time $\left(E_{1}, 2\right)=$ true
$\operatorname{actor}\left(E_{1}, J o h n\right)=$ true
object $\left(E_{1}, M a n\right)=$ true
act $\left(F_{1}\right.$, See $)=$ true
device $\left(E_{1}^{1}\right.$, Telescope $)=$ true
which means that the telescope is used as a device.
And. our HCLP language gives the following result for the sentences in Example 2:
time $\left(L_{1}, 2\right)=$ true
$\operatorname{actor}\left(E_{1}, J o h n\right)=$ true
$\operatorname{djject}\left(B_{1}, M a n\right)=$ true
act $\left(E_{1}, S c e\right)=$ truc
denice $\left(E_{1}\right.$, Telescope $)=$ false
actor $\left(L_{1}^{\prime}, M a n\right)=$ true
time $\left(E_{1}^{\prime}, 2\right)=$ true
$\operatorname{act}\left(E_{1}^{\prime}, H a v e\right)=\operatorname{truc}$
object $\left(E_{1}^{\prime}\right.$,Tclescope $)=$ true
which means that the man has the telescope (and it is not used as a device).

## 6 Conclusion

We believe that the following are contribntions of this paper.

1. We examine a feasibility of prioritized circumscription for specifying the most preferable reading by considering a disanbiguation task in the concrete examples and show that we can represent the task quite naturally.
2. We discuss an implementation of disambiguation within an HCLP language by showing a correspondence between a priority over preference rules in prioritized circomscription and a constrant hierarchy in HCLP.

As a future rescarch, we need the following.

1. We would like to examine a computational complexity of disambiguation by HCLP.
2. It is better to learn preferences antomatically in stead of specifying preferences by user. One approach for learning is to buikd an interactive system such that the system shows to a user a set of possible readings for given sentences and the user gives an order over possible readings. Then, the system would be able to learn preferences by generalizing the order.

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[^0]:    ${ }^{1}$ We ignore joint ownership for simplicity. If we would like to consider the possibility, we can represent the formula as the strongest preference.

